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MATHEMATICS ACHIEVEMENT IN THE
PRIMARY SCHOOL YEARS:
IEA'S THIRD INTERNATIONAL MATHEMATICS
AND SCIENCE STUDY (TIMSS)

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Contents

EXECUTIVE SUMMARY	1
INTRODUCTION	9
Which Countries Participated?	10
Table 1 TIMSS Countries Testing in the Primary Grades	11
Table 2 Information About the Grades Tested	13
What Was the Nature of the Mathematics Test?	14
How Do Country Characteristics Differ?	15
Table 3 Selected Demographic Characteristics of TIMSS Countries	16
Table 4 Public Expenditure on Education at Primary and Secondary Levels in TIMSS Countries	17
Figure 1 Centralization of Decision-Making Regarding Curriculum Syllabi	19
Figure 2 Centralization of Decision-Making Regarding Textbooks	20
Figure 3 Centralization of Decision-Making Regarding Examinations	21
CHAPTER 1: INTERNATIONAL STUDENT ACHIEVEMENT IN MATHEMATICS	23
What Are the Overall Differences in Mathematics Achievement?	23
Table 1.1 Distributions of Mathematics Achievement - Upper Grade (Fourth Grade)	24
Figure 1.1 Multiple Comparisons of Mathematics Achievement - Upper Grade (Fourth Grade)	25
Table 1.2 Distributions of Mathematics Achievement - Lower Grade (Third Grade)	28
Figure 1.2 Multiple Comparisons of Mathematics Achievement - Lower Grade (Third Grade)	29
What Are the Increases in Achievement Between the Lower and Upper Grades?	30
Table 1.3 Achievement Differences in Mathematics Between Lower and Upper Grades (Third and Fourth Grades)	31
What Are the Differences in Performance Compared to Three Marker Levels of International Mathematics Achievement?	32
Table 1.4 Percentages of Students Achieving International Marker Levels in Mathematics Upper Grade (Fourth Grade)	33
Table 1.5 Percentages of Students Achieving International Marker Levels in Mathematics Lower Grade (Third Grade)	34
What Are the Gender Differences in Mathematics Achievement?	35
Table 1.6 Gender Differences in Mathematics Achievement - Upper Grade (Fourth Grade)	36
Table 1.7 Gender Differences in Mathematics Achievement - Lower Grade (Third Grade)	37

What Are the Differences in Median Performance at Age 9?	38
Table 1.8 Median Mathematics Achievement of 9-Year-Old Students	39
How Does Fourth-Grade Performance Compare with Eighth-Grade Performance?	40
Figure 1.3 Mathematics Performance at Fourth and Eighth Grades Compared with the International Averages	41
Table 1.9 Increases in Mathematics Performance Between the Fourth and Eighth Grades	43
CHAPTER 2: AVERAGE ACHIEVEMENT IN THE MATHEMATICS CONTENT AREAS	45
How Does Achievement Differ Across Mathematics Content Areas?	45
Table 2.1 Average Percent Correct by Mathematics Content Areas - Upper Grade (Fourth Grade)	47
Table 2.2 Average Percent Correct by Mathematics Content Areas - Lower Grade (Third Grade)	48
Table 2.3 Profiles of Relative Performance in Mathematics Content Areas - Lower and Upper Grades (Third and Fourth Grades)	51
What Are the Increases in Achievement Between the Lower and Upper Grades?	52
Figure 2.1 Difference in Average Percent Correct Between Lower and Upper Grades (Third and Fourth Grades) Overall and in Mathematics Content Areas	54
What Are the Gender Differences in Achievement for the Content Areas?	56
Table 2.4 Average Percent Correct for Boys and Girls by Mathematics Content Areas Upper Grade (Fourth Grade)	58
Table 2.5 Average Percent Correct for Boys and Girls by Mathematics Content Areas Lower Grade (Third Grade)	60
CHAPTER 3: PERFORMANCE ON ITEMS WITHIN EACH MATHEMATICS CONTENT AREA	63
What Have Students Learned About Whole Numbers?	63
Table 3.1 Percent Correct for Example Item 1 - Lower and Upper Grades (Third and Fourth Grades)	66
Table 3.2 Percent Correct for Example Item 2 - Lower and Upper Grades (Third and Fourth Grades)	67
Table 3.3 Percent Correct for Example Item 3 - Lower and Upper Grades (Third and Fourth Grades)	68
Table 3.4 Percent Correct for Example Item 4 - Lower and Upper Grades (Third and Fourth Grades)	69
Table 3.5 Percent Correct for Example Item 5 - Lower and Upper Grades (Third and Fourth Grades)	70
Figure 3.1 International Difficulty Map for Whole Numbers Example Items	71
What Have Students Learned About Fractions and Proportionality?	72
Table 3.6 Percent Correct for Example Item 6 - Lower and Upper Grades (Third and Fourth Grades)	74
Table 3.7 Percent Correct for Example Item 7 - Lower and Upper Grades (Third and Fourth Grades)	75
Table 3.8 Percent Correct for Example Item 8 - Lower and Upper Grades (Third and Fourth Grades)	76

Table 3.9 Percent Correct for Example Item 9 – Lower and Upper Grades (Third and Fourth Grades)	77
Table 3.10 Percent Correct for Example Item 10 – Lower and Upper Grades (Third and Fourth Grades)	78
Figure 3.2 International Difficulty Map for Fractions and Proportionality Example Items	80
What Have Students Learned About Measurement, Estimation, and Number Sense?	81
Table 3.11 Percent Correct for Example Item 11 – Lower and Upper Grades (Third and Fourth Grades)	83
Table 3.12 Percent Correct for Example Item 12 – Lower and Upper Grades (Third and Fourth Grades)	84
Table 3.13 Percent Correct for Example Item 13 – Lower and Upper Grades (Third and Fourth Grades)	85
Table 3.14 Percent Correct for Example Item 14 – Lower and Upper Grades (Third and Fourth Grades)	86
Table 3.15 Percent Correct for Example Item 15 – Lower and Upper Grades (Third and Fourth Grades)	87
Figure 3.3 International Difficulty Map for Measurement, Estimation, and Number Sense Example Items	88
What Have Students Learned About Data Representation, Analysis, and Probability?	89
Table 3.16 Percent Correct for Example Item 16 – Lower and Upper Grades (Third and Fourth Grades)	91
Table 3.17 Percent Correct for Example Item 17 – Lower and Upper Grades (Third and Fourth Grades)	92
Table 3.18 Percent Correct for Example Item 18 – Lower and Upper Grades (Third and Fourth Grades)	94
Table 3.19 Percent Correct for Example Item 19 – Lower and Upper Grades (Third and Fourth Grades)	95
Table 3.20 Percent Correct for Example Item 20 – Lower and Upper Grades (Third and Fourth Grades)	96
Figure 3.4 International Difficulty Map for Data Representation, Analysis, and Probability Example Items	97
What Have Students Learned About Geometry?	98
Table 3.21 Percent Correct for Example Item 21 – Lower and Upper Grades (Third and Fourth Grades)	99
Table 3.22 Percent Correct for Example Item 22 – Lower and Upper Grades (Third and Fourth Grades)	100
Table 3.23 Percent Correct for Example Item 23 – Lower and Upper Grades (Third and Fourth Grades)	101
Table 3.24 Percent Correct for Example Item 24 – Lower and Upper Grades (Third and Fourth Grades)	102
Table 3.25 Percent Correct for Example Item 25 – Lower and Upper Grades (Third and Fourth Grades)	103
Figure 3.5 International Difficulty Map for Geometry Example Items	104
What Have Students Learned About Patterns, Relations, and Functions?	105
Table 3.26 Percent Correct for Example Item 26 – Lower and Upper Grades (Third and Fourth Grades)	106
Table 3.27 Percent Correct for Example Item 27 – Lower and Upper Grades (Third and Fourth Grades)	107
Table 3.28 Percent Correct for Example Item 28 – Lower and Upper Grades (Third and Fourth Grades)	108
Table 3.29 Percent Correct for Example Item 29 – Lower and Upper Grades (Third and Fourth Grades)	109
Table 3.30 Percent Correct for Example Item 30 – Lower and Upper Grades (Third and Fourth Grades)	110
Figure 3.6 International Difficulty Map for Patterns, Relations, and Functions Example Items	111

CHAPTER 4: STUDENTS' BACKGROUNDS AND ATTITUDES TOWARDS MATHEMATICS	113
What Educational Resources Do Students Have in Their Homes?	113
Table 4.1 Students' Reports on Educational Aids in the Home: Dictionary, Study Desk/Table, and Computer	114
Table 4.2 Students' Reports on the Number of Books in the Home	116
Table 4.3 Students' Reports on Frequency with Which They Speak the Language of the Test at Home	117
Table 4.4 Students' Reports on Whether or Not Their Parents Were Born in the Country	119
Table 4.5 Students' Reports on Whether or Not They Were Born in the Country	120
What Are the Academic Expectations of Students, Their Families, and Their Friends?	121
Table 4.6 Students' Reports on Whether They Think That It Is Important to Do Various Activities	123
Table 4.7 Students' Reports on Whether Their Mothers Think That It Is Important to Do Various Activities	124
Table 4.8 Students' Reports on Whether Their Friends Think That It Is Important to Do Various Activities	125
How Do Students Spend Their Out-of-School Time During the School Week?	126
Table 4.9 Students' Reports on the Amount of Out-of-School Time Spent Studying Mathematics or Doing Mathematics Homework on a Normal School Day	127
Table 4.10 Students' Reports on How They Spend Their Leisure Time on a Normal School Day	128
Table 4.11 Students' Reports on the Hours Spent Watching Television and Videos on a Normal School Day	130
How Do Students Perceive Success in Mathematics?	131
Table 4.12 Students' Self-Perceptions About Usually Doing Well in Mathematics	132
Figure 4.1 Gender Differences In Students' Self-Perceptions About Usually Doing Well in Mathematics	133
Table 4.13 Students' Reports on Things Necessary to Do Well in Mathematics	135
What Are Students' Attitudes Towards Mathematics?	136
Table 4.14 Students' Reports on How Much They Like Mathematics	137
Figure 4.2 Gender Differences in Liking Mathematics	138
Table 4.15 Students' Overall Attitudes Towards Mathematics	140
Figure 4.3 Gender Differences in Students' Overall Attitudes Towards Mathematics	141

CHAPTER 5: TEACHERS AND INSTRUCTION	143
Who Delivers Mathematics Instruction?	144
Table 5.1 Requirements for Certification Held by the Majority of Lower and Upper Grade Teachers	145
Table 5.2 Teachers' Reports on Their Age and Gender	146
Table 5.3 Teachers' Reports on Their Years of Teaching Experience	148
What Are Teachers' Perceptions About Mathematics?	149
Figure 5.1 Percentage of Students Whose Mathematics Teachers Agree or Strongly Agree with Statements About the Nature of Mathematics and Mathematics Teaching	150
Figure 5.2 Percent of Students Whose Mathematics Teachers Think Particular Abilities Are Very Important for Students' Success in Mathematics in School	152
How Do Mathematics Teachers Spend Their School-Related Time?	154
Table 5.4 Teachers' Reports on Average Number of Hours Mathematics Is Taught Weekly to Their Mathematics Classes	155
Figure 5.3 Percent of Students Who Are Taught Both Mathematics and Science by a Single Classroom Teacher	156
Table 5.5 Average Number of Hours Students' Teachers Spend on Various School-Related Activities Outside the Formal School Day During the School Week	157
Table 5.6 Teachers' Reports on How Often They Meet with Other Teachers in Their Subject Area to Discuss and Plan Curriculum or Teaching Approaches	158
How Are Mathematics Classes Organized?	159
Figure 5.4 Teachers' Reports on What Factors Limit How They Teach Class	160
Table 5.7 Teachers' Reports on Average Size of Mathematics Class	163
Figure 5.5 Teachers' Reports About Classroom Organization During Mathematics Lessons	164
What Activities Do Students Do in Their Mathematics Lessons?	166
Table 5.8 Teachers' Reports on Their Familiarity with National and Regional Mathematics Curriculum Guides	167
Table 5.9 Teachers' Reports on Their Main Sources of Written Information When Deciding Which Topics to Teach and How to Present a Topic	168
Figure 5.6 Teachers' Reports About Using a Textbook in Teaching Mathematics	169
Table 5.10 Teachers' Reports on How Often They Ask Students to Practice Computational Skills	170
Table 5.11 Teachers' Reports on How Often They Ask Students to Do Reasoning Tasks	172
Table 5.12 Students' Reports on Using Things from Everyday Life in Solving Mathematics Problems	173

How Are Calculators and Computers Used?	174
Table 5.13 Students' Reports on Having a Calculator and Computer in the Home	175
Table 5.14 Teachers' Reports on Frequency of Students' Use of Calculators in Mathematics Class	176
Table 5.15 Teachers' Reports on Ways in Which Calculators Are Used At Least Once or Twice a Week	177
Table 5.16 Students' Reports on Frequency of Using Calculators in Mathematics Class	178
Table 5.17 Teachers' Reports on Frequency of Using Computers in Mathematics Class to Solve Exercises or Problems	179
Table 5.18 Students' Reports on Frequency of Using Computers in Mathematics Class	180
What Homework Are Students Assigned?	181
Table 5.19 Teachers' Reports About the Amount of Mathematics Homework Assigned	182
Table 5.20 Teachers' Reports on Their Use of Students' Written Mathematics Homework	183
APPENDIX A: OVERVIEW OF TIMSS PROCEDURES: MATHEMATICS ACHIEVEMENT RESULTS FOR THIRD- AND FOURTH-GRADE STUDENTS	A-1
History	A-1
The Components of TIMSS	A-2
Figure A.1 Countries Participating in Additional Components of TIMSS Testing	A-4
Developing the TIMSS Mathematics Test	A-5
Figure A.2 The Three Aspects and Major Categories of the Mathematics Framework	A-7
Table A.1 Distribution of Mathematics Items by Content Reporting Category and Performance Category	A-8
TIMSS Test Design	A-9
Sample Implementation and Participation Rates	A-9
Table A.2 Coverage of TIMSS Target Population	A-11
Table A.3 Coverage of 9-Year-Old Students	A-12
Table A.4 School Participation Rates and Sample Sizes - Upper Grade (Fourth Grade)	A-13
Table A.5 Student Participation Rates and Samples Sizes - Upper Grade (Fourth Grade)	A-14
Table A.6 School Participation Rates and Sample Sizes - Lower Grade (Third Grade)	A-15
Table A.7 Student Participation Rates and Samples Sizes - Lower Grade (Third Grade)	A-16
Table A.8 Overall Participation Rates - Lower and Upper Grades (Third and Fourth Grades)	A-17
Indicating Compliance with Sampling Guidelines in the Report	A-18
Figure A.3 Countries Grouped for Reporting of Achievement According to Their Compliance With Guidelines for Sample Implementation and Participation Rates	A-19
Data Collection	A-20

Scoring the Free-Response Items	A-21
Table A.9 TIMSS Within-Country Free-Response Coding Reliability Data for Population 1 Mathematics Items	A-22
Test Reliability	A-23
Data Processing	A-23
Table A.10 Cronbach’s Alpha Reliability Coefficients – TIMSS Mathematics Test Lower and Upper Grades (Third and Fourth Grades)	A-24
IRT Scaling and Data Analysis.....	A-25
Estimating the Link Between Fourth- and Eighth-Grade Performance.....	A-26
Table A.11 Mathematics Performance at the Third, Fourth, Seventh, and Eighth Grades Based on the Population 2 (Seventh- and Eighth-Grade) Scale	A-27
Estimating Sampling Error	A-28
APPENDIX B: THE TEST-CURRICULUM MATCHING ANALYSIS	B-1
Table B.1 Test-Curriculum Matching Analysis Results – Mathematics – Upper Grade (Fourth Grade)	B-3
Table B.2 Test-Curriculum Matching Analysis Results – Mathematics – Lower Grade (Third Grade)	B-4
Table B.3 Standard Errors for the Test-Curriculum Matching Analysis – Upper Grade (Fourth Grade)	B-7
Table B.4 Standard Errors for the Test-Curriculum Matching Analysis – Lower Grade (Third Grade)	B-8
APPENDIX C: PERCENTILES AND STANDARD DEVIATIONS OF MATHEMATICS ACHIEVEMENT	C-1
Table C.1 Percentiles of Achievement in Mathematics – Upper Grade (Fourth Grade)	C-2
Table C.2 Percentiles of Achievement in Mathematics – Lower Grade (Third Grade)	C-3
Table C.3 Standard Deviations of Achievement in Mathematics – Upper Grade (Fourth Grade)	C-4
Table C.4 Standard Deviations of Achievement in Mathematics – Lower Grade (Third Grade)	C-5
APPENDIX D: ACKNOWLEDGMENTS	D-1

